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Densities of Aqueous Lithium, Sodium, and Potassium Hydroxides from 25 to 75 $^\circ\text{C}$ at 1 atm

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A weight dilatometer has been used to measure the densities of aqueous solutions of lithium, sodium, and potassium hydroxides up to 3 m at 10 °C intervals in the range 25–75 °C at 1.013 bar. The precision of the densities is $\pm 1 \times 10^{-5}$ g cm⁻³. The data are compared with literature values where applicable.

Introduction

In the conversion of fossil and nuclear energy to electricity high-temperature solution-phase thermodynamic data are required to improve plant reliability. For example, most corrosion problems in boiler water circuits arise where the solution can concentrate; the compositions of these concentrated solutions can only be obtained from thermochemical data. In order to obtain density data at high temperatures it is necessary to have a good knowledge of the density at lower temperatures. Currently there is a great lack of solution density data on alkalis at temperatures other than room temperature. In this work we have been interested in developing a technique which can be used to obtain data at atmospheric pressure and that can be relatively easily adapted to measuring densities under pressure at high temperatures. This technique is used to provide the basic low-temperature data for the high-temperature study.

Experimental Section

Materials. The alkali hydroxides used were AR grade. Carbonate-free solutions were prepared by precipitation of carbonate using the method described by Vögel (1). The carbonate-free hydroxide solutions were then stored under nitrogen in blacked-out plastic containers until use. The potassium hydrogen phthalate used for standardization was recrystallized 3 times from conductivity water after a hot filtration; it was then dried in the vacuum oven and stored under vacuum until use. All solutions were prepared by using demineralized water which was first distilled and then passed through a nuclear-grade mixed bed in-exchange resin, followed by a filter column until its conductivity was less than 0.05 μ S cm⁻¹. All mercury used was recovered and cleaned by a four-stage process, dried by passing air through it in contact with AR grade acetone, and stored under nitrogen in plastic containers until use.

All solutions were degassed by boiling under reduced pressure for $1/_2$ h before standardization. The hydroxide solutions were standarized by titration against weighed portions of a potassium hydrogen phthalate solution, which had been made up by weight, using a Metrohm 636 Titroprocessor in conjunction with a Metrohm E635 Dosimat unit. This procedure gave

Table I. Density of Wa	ater
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T/K	$ ho_0/\mathrm{g~cm^{-3}}$	T/K	$ ho_0/{ m g~cm^{-3}}$
298.15	0.997 048	328.15	0.985 696
308.15	0.994 035	338.15	0.980 553
318.15	0.990 216	348.15	0.974 844

a reproducibility of better than 0.005%.

Solutions were made up by weight and buoyancy corrections applied; the air density at the time of weighing was calculated from tables (2). Two balances were used during this work: first, a Stanton SM12 double pan balance, used in conjunction with a set of National Physical Laboratory (NPL) calibration stainless steel weights, and second, a Sartorius 2004 MP electronic balance. Both balances gave a precision of $\pm 2 \times 10^{-5}$ g and operated over a range of 0–160 g. The two balances agreed to within $\pm 1 \times 10^{-5}$ g on a given weight.

Dilatometer. The dilatometer used was similar in design to the weight dilatometer of Gibson and Loeffler (3), but was made of titanium. The opening for filling the dilatometer was made as narrow as possible and the flange was sealed by a flat plate clamped against a silicone rubber seating. The principle of operation is that mercury is diplaced through a capillary from the dilatometer and collected in a preweighed pot. The advantage of this method is that it allows a large number of measurements to be made over several temperatures without refilling the dilatometer, to give a precision of $\pm 1 \times 10^{-5}$ g cm⁻³. Values for the density of water were taken from Kell (4) (Table I) and for the density of mercury from ref 2. The temperature of the water thermostat was monitored with an NPL calibrated platinum resistance thermometer, in conjunction with an Automatic Systems Laboratories precision ac double transformer ratio bridge (Model H6), to $\pm 1 \times 10^{-3}$ K. Temperature control was better than $\pm 2 \times 10^{-3}$ K.

Results and Discussion

Values for the density of each electrolyte were obtained at 10-deg intervals between 25 and 75 °C, and over a 0.5–3 m concentration range. Measurements were not carried out below 0.5 m as a precision of $\pm 1 \times 10^{-5}$ g cm⁻³ in the density gives an error of ± 0.02 cm³ mol⁻¹ in the apparent molar volume at 0.5 m but ± 0.1 cm³ mol⁻¹ at 0.1 m. The results for lithium hydroxide, sodium hydroxide, and potassium hydroxide are given in Tables II–IV. The apparent molar volume of each solution was calculated from these data by using eq 1 (see Glossary at end of paper).

$${}^{\phi}V = \frac{1}{m}\left(\frac{1}{\rho} - \frac{1}{\rho_0}\right) + \frac{M_2}{\rho} \tag{1}$$

Table II. Densities of Lithium H	lvdroxide	Solutions
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			ρ/g	cm ⁻³		
$m/\mathrm{mol}\ \mathrm{kg}^{-1}$	298.15 K	308.15 K	318.15 K	328.15 K	338.15 K	348.15 K
0.4800	1.010 05	1.006 88	1.003 00	0.998 48	0.993 38	0.98777
0.7014	1.01587	1.01263	1.00872	1.00420	0.99912	0.993 54
0.9356	1.02191	1.01860	1.01466	1.01013	1.00507	0.999 52
1.1314	1.02687	1.02350	1.01953	1.01500	1.009 95	1.00443
1.3306	1.031 83	1.02840	1.02440	1.01987	1.01483	1.00933
1.3829	1.03311	1.02967	1.02567	1.021 13	1.016 09	1.01060
1.6851	1.04043	1.03691	1.03286	1.02831	1.02328	1.017 81
1.8532	1.04442	1.04085	1.03678	1.03221	1.02718	1.02174
2.2556	1.05371	1.05004	1.045 90	1.04131	1.03628	1.03086
2.2587	1.05378	1.05011	1.04597	1.04138	1.03635	1.030 93
2.5651	1.06061	1.05687	1.05269	1.04806	1.04302	1.03762
2.7892	1.06547	1.06168	1.05747	1.05282	1.04777	1.04237

Table III. Densities of Sodium Hydroxide Solutions

	$\rho/g \text{ cm}^{-3}$					
$m/{ m mol}~{ m kg}^{-1}$	298.15 K	308.15 K	318.15 K	328.15 K	338.15 K	348.15 K
0.5038	1.018 81	1.015 36	1.011 17	1.00645	1.00118	0.995 41
0.7483	1.02902	1.02538	1.02105	1.01622	1.01090	1.005 09
0.9999	1.039 30	1.03548	1.031 03	1.02610	1.02072	1.01488
1.2447	1.04911	1.04511	1.04056	1.03554	1.03012	1.02424
1.3534	1.05340	1.049 33	1.04474	1.03968	1.03423	1.02834
1.7039	1.06701	1.06272	1.05802	1.05283	1.04732	1.04138
2.0006	1.07828	1.07380	1.06901	1.06373	1.05817	1.05218
2.2447	1.087 39	1.08276	1.077 90	1.07255	1.066 94	1.06092
2.4929	1.09651	1.09174	1.086 80	1.081 40	1.07577	1.06969
2.7396	1.10547	1.10054	1.09552	1.09008	1.08441	1.07828
3.0094	1.11514	1.11005	1.10491	1.099 45	1.09376	1.08755

Table IV. Densities of Potassium Hydroxide Solutions

			ρ/g	cm ⁻³			
$m/\mathrm{mol}\ \mathrm{kg}^{-1}$	298.15 K	308.15 K	318.15 K	328.15 K	338.15 K	348.15 K	
0.4920	1.021 28	1.017 87	1.01378	1.009 10	1.003 82	0.998 04	
0.8058	1.03618	1.03255	1.02832	1.02353	1.01820	1.012 39	
0.9554	1.04313	1.03941	1.03511	1.030 28	1.024 93	1.01911	
1.1128	1.05036	1.04654	1.04218	1.037 29	1.031 92	1.02611	
1.3484	1.060 98	1.05704	1.05259	1.04763	1.04224	1.03642	
1.7145	1.077 09	1.07296	1.06840	1.06334	1.05790	1.05210	
1.7830	1.08005	1.075 89	1.07131	1.066 23	1.06078	1.054 98	
2.0344	1.09078	1.08650	1.08185	1.07672	1.07124	1.06545	
2.3453	1.10376	1.099 35	1.09463	1.08944	1.08391	1.07812	
2.5502	1.11216	1.10765	1.10290	1.097 69	1.09211	1.08631	
3.0211	1.131 00	1.126 29	1.121 46	1.11622	1.11051	1.10468	

Table V. Fitting Parameters for Lithium Hydroxide

T/\mathbf{K}	${}^{\phi}V^{\infty}/\mathrm{cm}^3 \mathrm{\ mol}^{-1}$	$10^5 (\partial \beta^{\circ} / \partial P) / \text{kg mol}^{-1} \text{ atm}^{-1}$	$rac{10^5(\partialeta^1/\partial P)/}{\mathrm{kg}^2~\mathrm{mol}^{-2}~\mathrm{atm}^{-1}}$	$rac{10^6 (\partial C^{\phi}/\partial P)}{ m kg^2\ mol^{-2}\ atm^{-1}}$	std dev of fit
298.15	-4.287 ± 0.012	-0.111 ± 0.091	3.759 ± 0.251	-0.335 ± 0.185	0.002
308.15	-4.103 ± 0.008	-0.384 ± 0.057	3.986 ± 0.159	-0.253 ± 0.117	0.001
318.15	-4.128 ± 0.010	-0.760 ± 0.072	4.670 ± 0.200	-0.477 ± 0.147	0.002
328.15	-4.327 ± 0.010	-1.052 ± 0.072	5.109 ± 0.201	-0.313 ± 0.148	0.002
338.15	-4.619 ± 0.013	-1.615 ± 0.085	6.283 ± 0.236	-0.584 ± 0.174	0.002
348.15	-5.168 ± 0.013	-1.469 ± 0.084	5.748 ± 0.232	-0.098 ± 0.171	0.002

The apparent molar volume data were smoothed by fitting to an extended form of the Debye-Hückel equation derived by Pitzer (5):

$${}^{\phi}V - [{}^{\phi}V^{\text{st}} - {}^{\phi}V^{\infty}] = {}^{\phi}V^{\infty} + 2RTm \left(\frac{\partial\beta^{0}}{\partial P}\right)_{T} + \frac{4RTm}{\alpha^{2}} \left(\frac{\partial\beta^{1}}{\partial P}\right)_{T} [1 - (1 + \alpha m^{1/2})e^{-\alpha m^{1/2}}] + RTm^{2} \left(\frac{\partial C^{\phi}}{\partial P}\right)_{T}$$

where

$${}^{\phi}V^{\rm st} - {}^{\phi}V^{\infty} = (A_{\rm v}/b) \ln (1 + bm^{1/2})$$
 (2)

 $b = 1.2 \text{ kg}^{1/2} \text{ mol}^{-1/2}$ and $\alpha = 2.0 \text{ kg}^{1/2} \text{ mol}^{-1/2}$. A_v is the Debye-Hückel slope and the values were taken from Bradley

and Pitzer (6). The values of the fitting parameters were obtained by nonlinear regression and are given in Tables V–VII.

Values of ${}^{\phi}V$ (smoothed) at very low concentrations were calculated from the fitting parameters. The relative apparent molar volume ${}^{\phi}V^{\text{rel}} = {}^{\phi}V$ (smoothed) $- {}^{\phi}V^{\infty}$) is plotted against $m^{1/2}$ at 25 °C in Figure 1. As $m^{1/2}$ tends to zero the slope approaches A_v/b (7). Sodium and potassium hydroxides show a small positive deviation whereas lithium hydroxide has a marked negative deviation. With increasing temperature all the hydroxides show negative deviations.

The values for the apparent molar volume at infinite dilution, ${}^{\phi}V^{\infty}$, were compared where possible with existing literature data. Where sufficient data are available, the quoted results were fitted to eq 2.

(a) Lithium Hydroxide. A difference of $1.7 \text{ cm}^3 \text{ mol}^{-1}$ is observed between the value of $-4.29 \text{ cm}^3 \text{ mol}^{-1}$ determined in

Table VI. Fitting Parameters for Sodium Hydroxide

dev of fit
0.003
0.003
0.003
0.001
0.003
0.002
-

Table VII. Fitting Parameters for Potassium Hydroxide

T/K	${}^{\phi}V^{\infty}/\mathrm{cm}^3 \mathrm{\ mol}^{-1}$	$\frac{10^{5}(\partial \beta^{\circ}/\partial P)}{\mathrm{kg \ mol^{-1} \ atm^{-1}}}$	$10^5(\partialeta^1/\partial P)/{ m kg^2\ mol^{-2}\ atm^{-1}}$	$rac{10^6 (\partial C^{\phi}/\partial P)}{ m kg^2 \ mol^{-2} \ atm^{-1}}$	std dev of fit
298.15	5.082 ± 0.020	1.592 ± 0.146	3.620 ± 0.387	-5.411 ± 0.249	0.004
308.15	5.780 ± 0.008	0.953 ± 0.055	3.767 ± 0.147	-4.054 ± 0.094	0.001
318.15	6.197 ± 0.023	0.254 ± 0.155	4.542 ± 0.413	-3.765 ± 0.265	0.004
328.15	6.254 ± 0.019	0.119 ± 0.129	4.585 ± 0.342	-4.075 ± 0.220	0.003
338.15	6.394 ± 0.023	-1.024 ± 0.146	6.350 ± 0.387	-3.304 ± 0.249	0.004
348.15	6.243 ± 0.015	-1.281 ± 0.093	5.959 ± 0.246	-1.730 ± 0.158	0.003



Figure 1. Comparison of ${}^{\phi}V^{rel}$ for the alkali hydroxides at 25 °C.

this work for ${}^{\phi}V^{\infty}$ at 25 °C and the value of -6.0 cm³ mol⁻¹ recorded by Gucker (\mathcal{B}). Gucker's value is, however, based on the work of Lanman and Mair (\mathcal{P}), who quote only three density measurements for solutions between 0.5 and 2.2 *m* and no experimental details of the method used in their determination. The lack of data made it impossible to carry out a check analysis using the Pitzer equation. Recently Roux et al. (10) have used the vibrating tube method to determine the density of aqueous LiOH at 25 °C over the range 0.04–3.8 *m* and at 55 °C over the range 0.1–3.8 *m*. A comparison is made of the apparent molar volumes at rounded values of the molality in Table VIII. The smoothed values (b) quoted from ref 10 were calculated from their fitting parameters for a polynomial in $m^{1/2}$. As can be seen from Table VIII, the magnitudes of

Table VIII. Comparison of Smoothed Values^a of $^{\diamond}V$ for LiOH, NaOH, and KOH at 25 and 55 °C

	$^{\phi}V/\mathrm{cm}^{3} \mathrm{mol}^{-1}$					
		25 °C			55 °C	
$m/mol \ kg^{-1}$	(a)	(b)	(c)	(a)	(b)	(c)
			LiOH			
0.0	-4.29	-5.06	-4.96	-4.33	-5.05	-5.01
0.5	-3.17	-3.02	-3.04	-3.05	-2.88	-2.87
1.0	-2.57	-2.21	-2.19	-2.44	-2.01	-2.01
1.5	-2.01	-1.61	-1.57	-1.86	-1.41	-1.42
2.0	-1.46	-1.09	-1.07	-1.30	-0.93	-0.93
2.5	-0.92	-0.61	-0.62	-0.75	-0.51	-0.50
3.0	-0.40	-0.16	-0.19	-0.21	-0.10	-0.08
NaOH						
0.0	-4.90	-5.26	-5.46	-3.39	-3.39	-3.42
0.5	-3.28	-3.32	-3.32	-1.79	-1.62	-1.60
1.0	-2.30	-2.25	-2.20	-0.96	-0.76	-0.74
1.5	-1.44	-1.37	-1.33	-0.24	-0.04	-0.03
2.0	-0.68	-0.60	-0.58	0.41	0.61	0.60
2.5	-0.01	0.10	-0.09	0.99	1.21	1.18
3.0	0.56	0.74	0.70	1.50	1.76	1.73
]	кон			
0.0	5.08	4.92	4.83	6.25	6.25	6.17
0.5	6.58	6.74	6.79	7.79	7.99	8.01
1.0	7.48	7.72	7.78	8.58	8.80	8.83
1.5	8.29	8.52	8.55	9.29	9.46	9.49
2.0	9.03	9.22	9.21	9.92	10.05	10.07
2.5	9.68	9.85	9.80	10.49	10.60	10.59
3.0	10.27	10.42	10.34	10.99	11.10	11.08

^a a = this work; b = ref 10 (their parameters); c = ref 10 (Pitzer parameters).

the ${}^{\phi}V^{\infty}$ value from this work are less than theirs by 0.7 cm³ mol⁻¹ although at the higher concentrations our ${}^{\phi}V$ is from 0.1 to 0.3 cm³ mol⁻¹ larger at both temperatures. The data from ref 10 were also analyzed by using the Pitzer equation; these smoothed values are given in column (c) in Table VIII. It can be seen that the method of smoothing the data affects ${}^{\phi}V^{\infty}$ by 0.1–0.2 cm³ mol⁻¹.

(b) Sodium Hydroxide. Reported values of ${}^{\phi}V^{\infty}$ for sodium hydroxide at 25 °C lie in a range from -6.80 to -4.60 cm³ mol⁻¹ and are shown in Table IX. Our value of -4.90 cm³ mol⁻¹ lies to one end of this range among the determinations made at very low concentrations. The value of Alkerlöf and Kegeles (16) was obtained from high-concentration data and also no measurements were actually made at 25 °C; the tabulated value was obtained by least-squares analysis from data obtained at 10-deg intervals between 0 and 100 °C. Values 7 and 8 in Table IX were both based on the work of Lanman and Mair (9), which consisted of only three measurements. The work of Hepler et al. (13) quoted enough data for analysis using the

Table IX. Values of ${}^{\phi}V^{\circ}$ for NaOH at 25 °C

	$^{\phi}V^{\infty}/\mathrm{cm}^{3}$	method of	concn range/	
no.	mol^{-1}	measurement	mol kg ⁻¹	source
1	-4.60	dilatometer	0.006–0.65	Bodanszky and Kauzmann
2	-4.90	weight dilatometer	0.5-3.0	this work
3	-5.19	magnetic float	0.001-1.02	Millero et al. (12)
4	-5.25	dilatometer	0.002-0.85	Hepler et al. (13)
5	-5.26	vibrating tube	0.03–10.9	Roux et al. (10)
6	-5.37	vibrating tube	0.19–0.37	Allred and Woolley (14)
7	-5.42	pressure transducer	0.01-0.15	Swarin and Curran (15)
8	-5.94	pycnometer	1–26	Akerlöf and Kegeles (16)
9	-6.48	unknown	0.5 - 2.2	Lanman and Mair (9)
10	-6.80	calcd from ref 9		Owen and Brinkley (17)

Table X. Values of ^{\$V^*} for KOH at 25 °C

no.	${}^{\phi}V^{\infty}/\mathrm{cm}^3$ mol^{-1}	method of measurement	concn range/ mol kg ⁻¹	source
1	5.08	weight dilatometer	0.5-3.0	this work
2	4.92	vibrating tube	0.02 - 15.5	Roux et al. (10)
3	4.06	pycnometer	1-17	Akerlöf and Bender (18)
4	3.6	calcd from ref 18		Fajans and Johnson (19)
5	3.4	no source of data quoted		Owen and Brinkley (17)
6	2.9	calcd from ref 9		Gucker (8)

Pitzer equation: this showed perfect agreement with their reported value of -5.25 cm³ mol⁻¹. Although our value of ${}^{\phi}V^{\infty}$ at 25 °C differs from that of Roux et al. (10) by 0.4 cm³ mol⁻¹ it can be seen from Table VIII that very good agreement is obtained for ^{\$V} over the range 0.5-3.0 m; at 55 °C perfect agreement is obtained for ${}^{\phi}V^{\infty}$ (Table VIII) although at higher concentrations it is only ± 0.2 cm³ mol⁻¹.

(c) Potassium Hydroxide. Values of $^{\phi}V^{\infty}$ at 25 °C ranging from 2.9-4.92 cm³ mol⁻¹ have been reported and are shown in Table X. The value of 5.08 cm³ mol⁻¹ found in this work is significantly higher than the other reported values. Value No. 3 in the table is based on a least-squares analysis of data measured at 10-deg intervals between 0 and 100 °C and so no comparison of basic data is possible. Measurement 4 is reported as being based on the data of Akerlöf and Bender (18). No source of data is quoted for value 5. The lowest value shown, No. 6, is based on only three measurements of Lanman and Mair (9). Comparing ϕV at rounded molalities, over the experimental molality range, with the data of Roux et al. (10) (Table VIII), it can be seen that although our ${}^{\phi}V^{\infty}$ value at 25 °C is greater by 0.2 cm³ mol⁻¹ at higher concentrations our apparent molal volumes are less by 0.15-0.25 cm³ mol⁻¹. Exact agreement is obtained for ${}^{\phi}V^{\infty}$ at 55 °C (Table VIII) but over the molality range 0.5-3.0 covered by both sets of experimental measurements, the ϕV values differ by 0.1–0.2 cm³ mol⁻¹.

Glossary

Av	Debye-Hückel slope
M ₂	molar mass of solute
m	molality of solute
¢V	apparent molar volume
¢V∞	apparent molar volume at infinite dilution
${}^{\phi}V^{rel}$	${}^{\phi}V$ (smoothed) – ${}^{\phi}V^{\infty}$
ρ	density of solution
ρ_0	density of water

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Registry No. KOH. 1310-58-3; NaOH. 1310-73-2; LiOH. 1310-65-2.

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